

Integrating Powers of Trig Functions

"Answer Key"

$$1. \int \sin^2(2\theta) d\theta = \frac{1}{2}\theta - \frac{1}{8}\sin(4\theta) + M$$

$$2. \int \cos^2(3\theta) d\theta = \frac{1}{2}\theta + \frac{1}{12}\sin(6\theta) + N$$

$$3. \int \sin^7 \theta d\theta = -\frac{35}{64}\cos\theta + \frac{7}{64}\cos(3\theta) - \frac{7}{320}\cos(5\theta) + \frac{1}{448}\cos(7\theta) + O$$

$$4. \int \cos^5 \theta \sin^2 \theta d\theta = \frac{157}{840}\sin^3 \theta + \frac{9}{70}\sin^3 \theta \cos(2\theta) + \frac{1}{56}\sin^3(\theta) \cos(4\theta) + P$$

$$5. \int \cos^3 \theta \sin^3 \theta d\theta = \frac{1}{192}\cos(6\theta) - \frac{3}{64}\cos(2\theta) + Q$$

$$6. \int \sin^4 x dx = \frac{3}{8}x - \frac{1}{4}\sin(\frac{2x}{2}) + \frac{1}{32}\sin(4x) + R$$

$$7. \int \sec^6(2\theta) d\theta = \frac{4}{15}\tan(2\theta)\sec^4(2\theta) + \frac{1}{5}\cos(4\theta)\tan(2\theta)\sec^4(2\theta) + \frac{1}{30}\cos(8\theta)\tan(2\theta) + \sec^4(2\theta) + S$$

$$8. \int \tan^3 \theta d\theta = \frac{1}{2}\sec^2(x) + \ln|\cos(x)| + T$$

$$9. \int \sec(3\theta) d\theta = \frac{1}{3}\ln\left|\sin\left(\frac{3}{2}x\right) + \cos\left(\frac{3}{2}x\right)\right| - \frac{1}{3}\ln\left|\cos\left(\frac{3}{2}x\right) - \sin\left(\frac{3}{2}x\right)\right| + U$$

$$10. \int \tan^4 \theta \sec^4 \theta d\theta = \frac{6}{35}\tan^5(x)\sec^2(x) + \frac{1}{35}\cos(2x)\tan^5(x)\sec^2(x) + V$$

$$11. \int \tan \theta \sec^3 \theta d\theta = \frac{\sec^3(\theta)}{3} + W$$

$$12. \int \sec^4 \theta \tan^5 \theta d\theta = \frac{\sec^8(\theta)}{8} - \frac{\sec^6(\theta)}{3} + \frac{\sec^4(\theta)}{4} + A$$

$$13. \int \cos^4 \theta \sin^4 \theta d\theta = \frac{3}{128}\theta - \frac{1}{128}\sin(4\theta) + \frac{1}{1024}\sin(8\theta) + B$$